

Computational chemistry at the petascale: tools in the tool box



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SciDAC

Scientific Discovery through Advanced Computing

Chemical Computations on Future High-end Computers

Award #CHE 0626354, NSF Cyber Chemistry

- NCSA (T. Dunning, PI)
- U. Tennessee (Chemistry, EE/CS)
- U. Illinois UC (Chemistry)
- U. Pennsylvania (Chemistry)
- Conventional single processor performance no longer increasing exponentially
 - Multi-core
- Many “corners” of chemistry will increasingly be best served by non-conventional technologies
 - GP-GPU, FPGA, MD Grape/Wine

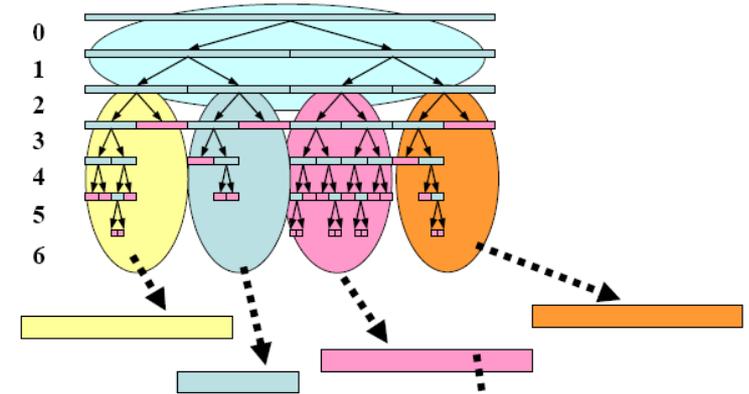
Award No:
NSF CNS-0509410

Project Title:
Collaborative research: CAS-AES: An integrated framework for compile-time/run-time support for multi-scale applications on high-end systems

Investigators:
P. Sadayappan (PI) G. Baumgartner, D. Bernholdt, R.J. Harrison, J. Nieplocha, J. Ramanujam and A. Rountev

Institution:
The Ohio State University
Louisiana State University
University of Tennessee, Knoxville

Website:
<http://www.cse.ohio-state.edu/~saday/>



```
class TaskMult : public TaskLeaf<TaskMult>
private:
    Future a, b;
public:
    TaskMult(Tree node, Function f,
             Function g, Function result)
        a = f.get(node)
        b = g.get(node)
    bool probe()
        return a.probe() and b.probe()
    bool predicate()
        return a.exists() and b.exists()
    void apply()
        multiply(node, a.get(), b.get())
```

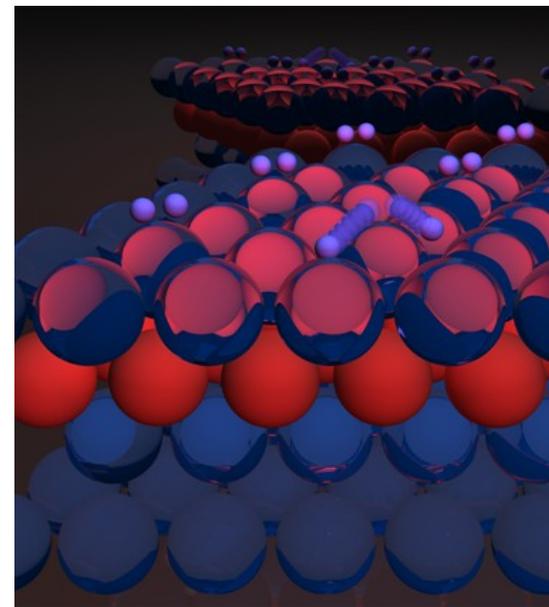
Description of Graphic Image:
A tree-based algorithm (here in 1D, but in actuality in 3-12D) is naturally implemented via recursion. The data in subtrees is managed in chunks and the computation expressed very compactly.

Science Opportunities

- The chemical industry represents 10% of all U.S. manufacturing, employing more than one million Americans.
- These fields require petascale computing coordinated with experimental programs for significant innovation
- Clean energy innovations for automobiles and industry (catalysis, fuel cells, combustion).
 - Catalysts design is presently a misnomer ... it is an Edisonian process
 - Only theory+advanced computing can enable rational design
 - Catalytic processes are directly involved in the synthesis of 20% of all industrial products.
- Molecular models for biological processes (protein and membrane function).
 - Modeling excited electronic states in photochemical systems and averaging over dynamics of the macromolecular structure potentially over very long timescales.
- Heavy element chemistry for advanced fuel cycles and environmental restoration.
 - These are special responsibilities of the DOE and petascale chemistry can replace many expensive experiments, and shorten timescales from decades to years.
- Dynamics of atoms and molecules interacting with electrons and powerful laser fields.
 - These are fundamental and defining challenges in physics and chemistry for the 21st century, and have been seeking for a solution for more than 50 years.
 - All major advances in this field are a result of new computational capabilities

Computational catalysis

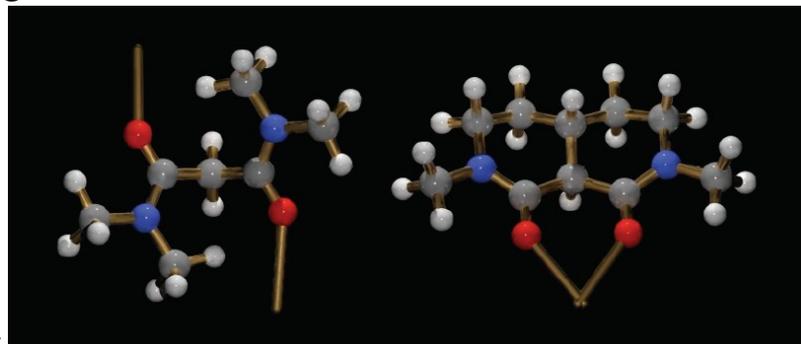
- Currently allocated 6+M hours between NCCS, NERSC, EMSL
 - Need a sustained 10-100x increase
- Approach
 - Large systems accurately described with *modern* hybrid and meta DFT functionals
 - Chemistry codes have the advantage here
 - Full petascale simulation only for the largest runs
 - Higher-accuracy necessary for quantitative rates and for calibration on smaller systems
 - Many-body methods – demonstrated scaling to 10K processors and predicted to go to 100+K
 - 75% of peak speed on EMSL HP cluster 1700 cpu
- Outcomes
 - Rational design of novel catalyst(s)
 - Future savings of \$B in various industries
 - Cleaner energy sources



Mavrikakis, Wisconsin.
H₂ dissociation path on a bimetallic NSA surface.

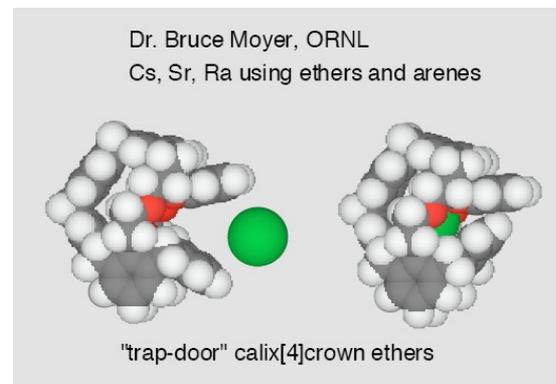
The role of simulation in heavy element chemistry for advanced fuel cycles

- Molecular-scale knowledge is vital to enable the rational design of new/enhanced agents
 - Reduced cost & risk with increased efficiency
 - Current experimental approach can generate only a fraction of required data over many years
 - The rest are guesstimated.
 - We can compute much of this
 - Need higher precision than currently feasible
 - Combinatorial methods use thermodynamics for screening, but this is not reliable enough



B. Hay, EMSP project 73759

- Approach
 - Mixed MM/QM Gibbs-free energy computations of partition coefficients
 - Simulation of select liquid-liquid, gas-gas interfaces
 - Accurate thermo-chemistry and spectroscopy
 - Many-body methods incorporating relativistic effects
- Outcomes
 - Design of new separation chemistries on a timescale relevant to engineering requirements (months to years rather than decades)



Issues

- Eliminate gulf between theoretical innovation in small groups and realization on high-end computers
- Eliminate the semantic gap so that efficient parallel code is no harder than doing the math
- Hardware/software architecture and programming models for 20xx
- Feasibility, support and maintenance

Major Molecular Electronic Structure Packages

- MOLPRO, MOLCAS, Turbomol, NWChem, GAMESS-US, GAMESS-UK, Gaussian, Jaguar, MPQC, ACES, QChem
- Wide range of functionality and algorithms
- Applicable to much of chemistry
- Vary greatly in speed, robustness, scalability, methods, ...
- Several codes often used within any one project
- circa 20M lines of code ...

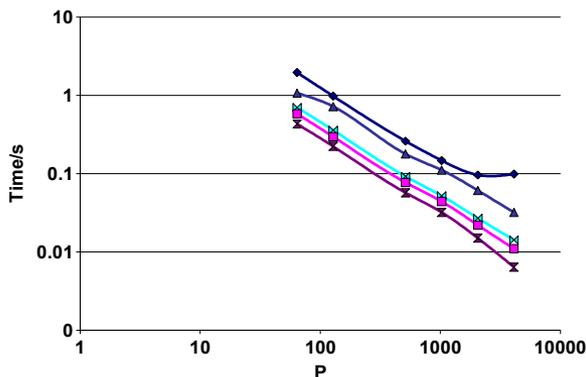
Computational Chemistry Endstation

Open, international collaboration: 8 universities & 5 national labs

- Led out of UT/ORNL
- Focus
 - Actinides, Aerosols, Catalysis
- ORNL Cray XT3, ANL BGL

Capabilities:

- Chemically accurate thermochemistry
 - Many-body methods required
- Mixed QM/QM/MM dynamics
 - Accurate free-energy integration
 - Simulation of extended interfaces
- Families of relativistic methods



Scaling of MADNESS 64-4096 cpu on XT3

NWChem: Largest CCSD(T) calculation

- Pollack, PNNL/EMSL, 2005.
- 1960 processor Itanium2 cluster
- 1468 basis functions (aug-cc-pVQZ)
- Perturbative triples (T)
 - 23 hours on 1400 processors
 - 75% of peak = 6.3 TFlops.

Trends in Chemistry Codes - I

- *All* scalable codes use one-sided communication in various forms
 - Ease of programming; increased scalability
- QM/MM, multi-scale methods, direct dynamics, ...
 - Multi-physics methods present scalability challenges
- Multi-level methods (FMM, multi-resolution, multi-grid, mixed-bases) in both space and time
 - A path to (near) linear or optimal scaling without sacrificing accuracy
 - Fully numerical real space methods
- Gaussian bases becoming attractive alternative to plane waves at low/medium precision? (Hütter)

Molecular Science Software Project



PNNL

**Yuri Alexeev,
Eric Bylaska,
Bert deJong,
Mahin Hackler,
Karol Kowalski,
Lisa Pollack,
Tjerk Straatsma,
Marat Valiev,
Theresa Windus**

ORNL

**Edo Apra,
Robert Harrison
Vincent Meunier
Ricky Kendall**



MS³

MOLECULAR SCIENCE
SOFTWARE SUITE



ECCE

EXTENSIBLE COMPUTATIONAL
CHEMISTRY ENVIRONMENT



NWChem

HIGH-PERFORMANCE COMPUTATIONAL
CHEMISTRY SOFTWARE



Ames
TL Windus

GA TOOLS

PARALLEL COMPUTING LIBRARIES
AND SOFTWARE TOOLS

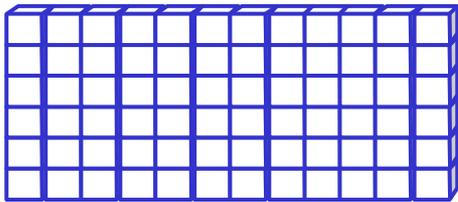
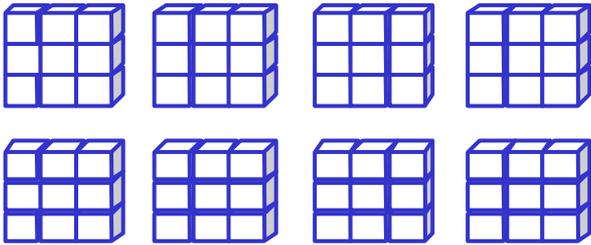
**Manoj Krishnan, Jarek Nieplocha,
Bruce Palmer, Vinod Tipparaju**



**Gary Black,
Brett Didier,
Todd Elsenthagen,
Sue Havre,
Carina Lansing,
Bruce Palmer,
Karen Schuchardt,
Lisong Sun
Erich Vorpapel**

Global Arrays

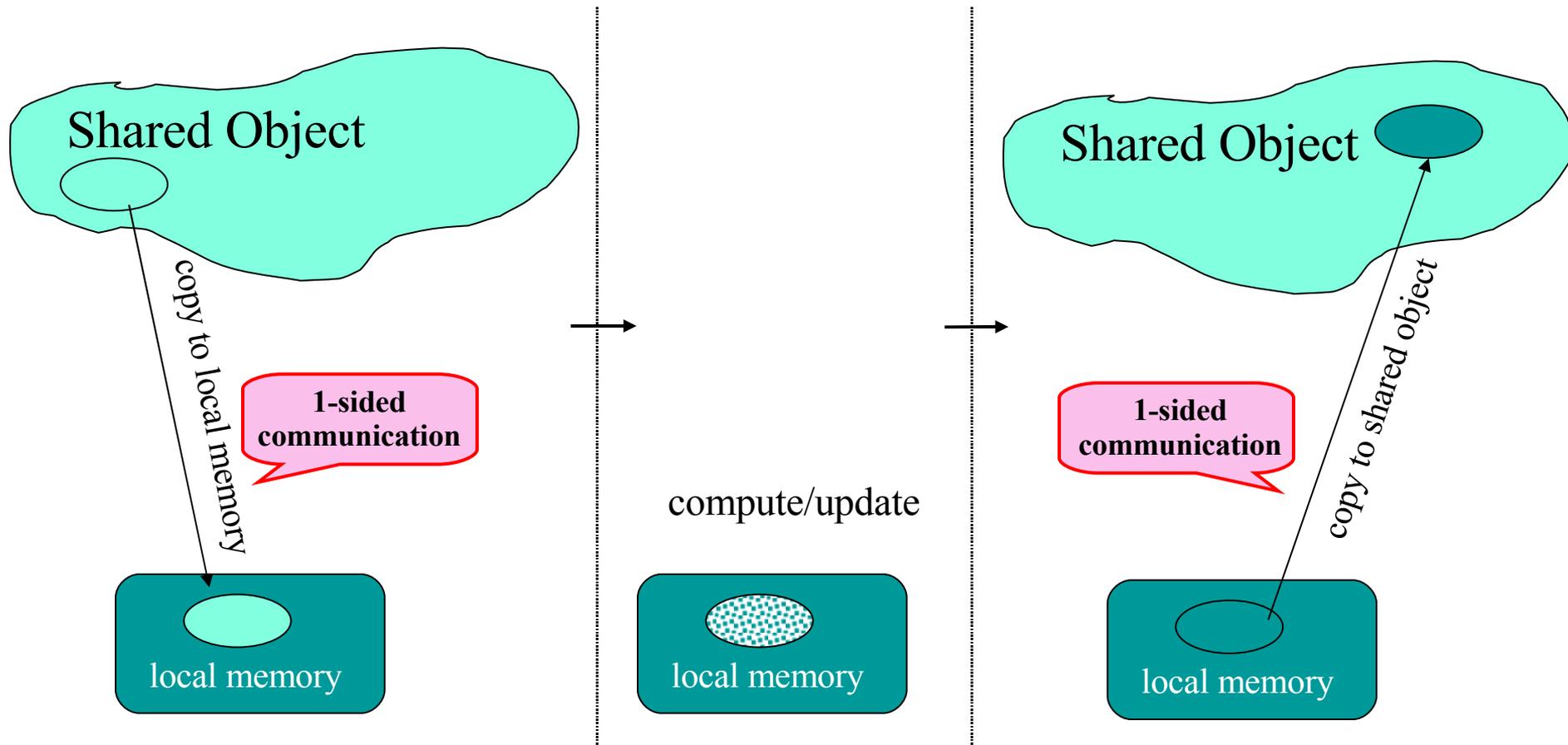
Physically distributed data



Single, shared data structure

- Shared-memory-like model
 - Fast local access
 - NUMA aware and easy to use
 - MIMD and data-parallel modes
 - Inter-operates with MPI, ...
- BLAS and linear algebra interface
- Ported to major parallel machines
 - IBM, Cray, SGI, clusters,...
- Originated in an HPC project
- Used by most major chemistry codes, financial futures forecasting, astrophysics, computer graphics
- Supported by DOE
- Jarek Nieplocha, PNNL

Non-uniform memory access model of computation



Dynamic load balancing

While ((task = SharedCounter()) < max)

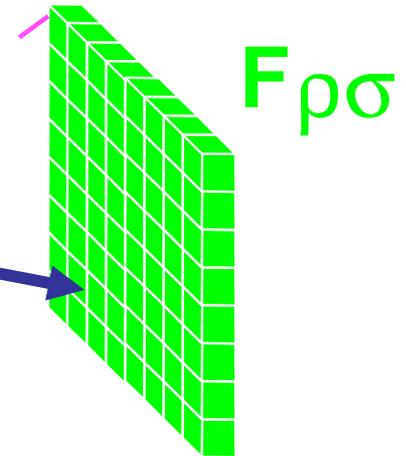
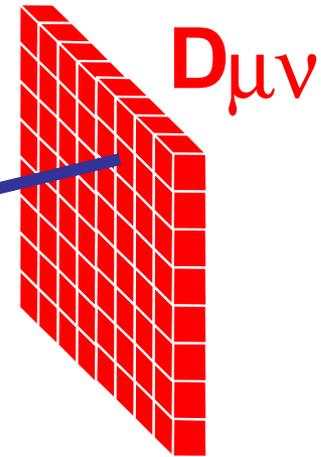
call ga_get()

(do work)

call ga_acc()

End while

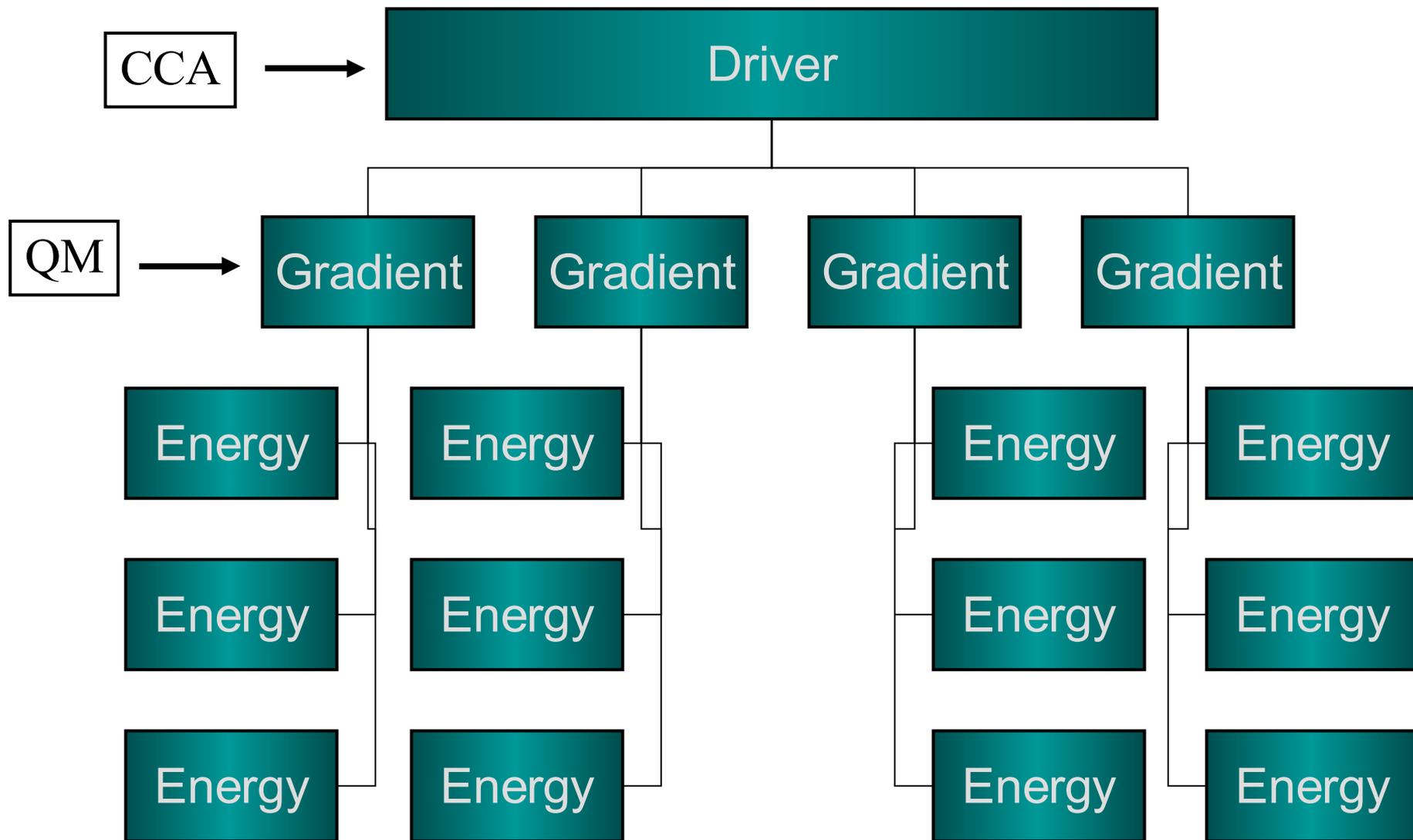
Barrier()



Trends in Chemistry Codes - II

- Multi-level parallelism
 - An effective path for most applications to scale to 100K processors without vast effort
 - Coarse grain over vibrational degrees of freedom in numerical hessian, or geometries in a surface scan or parameter study
 - Conventional distributed memory within each subtask
 - Fine grain parallelism within a few processor SMP (multi-threads, OpenMP, parallel BLAS, ...)
 - Efficient exploitation of fine grain parallelism is a major concern on future architectures
- MADNESS side steps some of these issues
- Community effort to increase interoperability and leverage new capabilities between codes
 - CCA being adopted

Numerical Hessians



Synthesis of High Performance Algorithms for Electronic Structure Calculations

<http://www.cis.ohio-state.edu/~gb/TCE>

- Collaboration between DOE/SciDAC, NSF/ITR and ORNL/LDRD
- Objective: develop a high level programming tool that translates many-body quantum theory into efficient massively parallel codes. This is anticipated to revolutionize the rate of progress in this field by eliminating man-years of programming effort.
- NSF Project:
 - Sadayappan (PI), Baumgartner, Cociorva, Pitzer (OSU)
 - Bernholdt, Harrison (unfunded) (ORNL)
 - Ramanujam (LSU)
 - Nooijen (Waterloo)
- DOE SciDAC: Harrison (PI), Hirata (PNNL)
- DOE ORNL/LDRD: Bernholdt (PI, 2002-3)
- Other SciDAC projects adopting this tool: Piecuch, Gordon
- Also being applied to nuclear physics (Bernholdt and Dean)

CCSD Doubles Equation

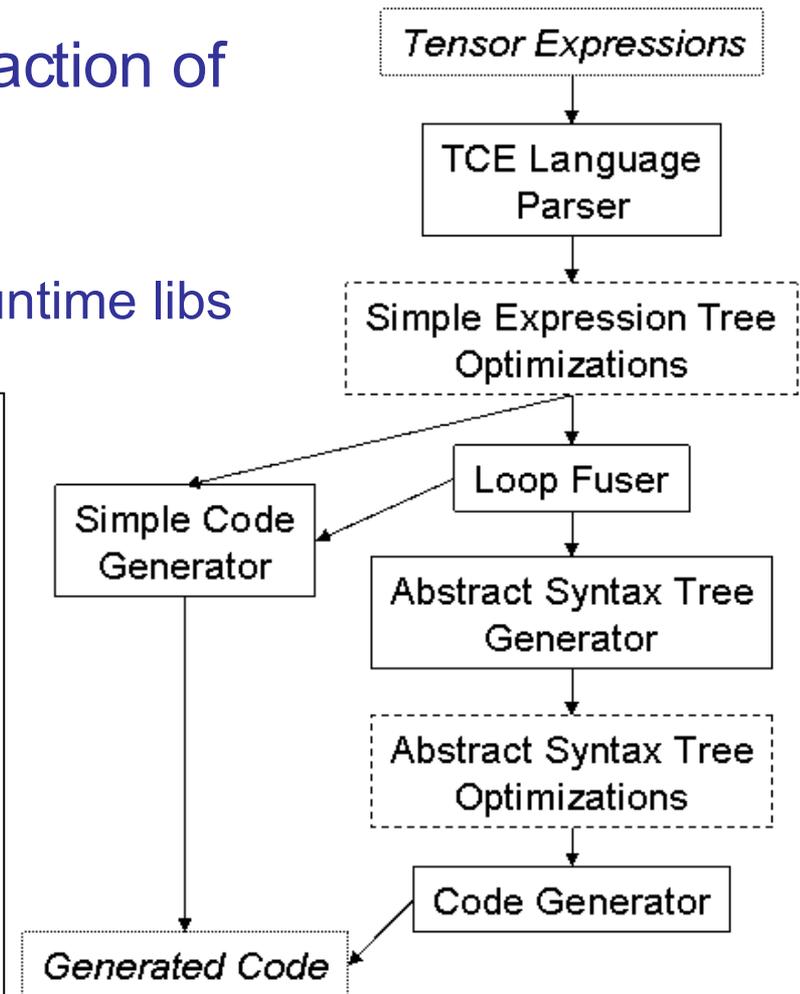
$$\begin{aligned} \text{hbar}[a,b,i,j] = & \text{sum}[f[b,c]*t[i,j,a,c],\{c\}] - \text{sum}[f[k,c]*t[k,b]*t[i,j,a,c],\{k,c\}] + \text{sum}[f[a,c]*t[i,j,c,b],\{c\}] - \text{sum}[f[k,c]*t[k,a]*t[i,j,c,b],\{k,c\}] \\ & - \text{sum}[f[k,j]*t[i,k,a,b],\{k\}] - \text{sum}[f[k,c]*t[j,c]*t[i,k,a,b],\{k,c\}] - \text{sum}[f[k,i]*t[j,k,b,a],\{k\}] - \text{sum}[f[k,c]*t[i,c]*t[j,k,b,a],\{k,c\}] \\ & + \text{sum}[t[i,c]*t[j,d]*v[a,b,c,d],\{c,d\}] + \text{sum}[t[i,j,c,d]*v[a,b,c,d],\{c,d\}] + \text{sum}[t[j,c]*v[a,b,i,c],\{c\}] - \text{sum}[t[k,b]*v[a,k,i,j],\{k\}] \\ & + \text{sum}[t[i,c]*v[b,a,j,c],\{c\}] - \text{sum}[t[k,a]*v[b,k,j,i],\{k\}] - \text{sum}[t[k,d]*t[i,j,c,b]*v[k,a,c,d],\{k,c,d\}] - \text{sum} \\ & [t[i,c]*t[j,k,b,d]*v[k,a,c,d],\{k,c,d\}] - \text{sum}[t[j,c]*t[k,b]*v[k,a,c,i],\{k,c\}] + 2*\text{sum}[t[j,k,b,c]*v[k,a,c,i],\{k,c\}] - \text{sum} \\ & [t[j,k,c,b]*v[k,a,c,i],\{k,c\}] - \text{sum}[t[i,c]*t[j,d]*t[k,b]*v[k,a,d,c],\{k,c,d\}] + 2*\text{sum}[t[k,d]*t[i,j,c,b]*v[k,a,d,c],\{k,c,d\}] - \text{sum} \\ & [t[k,b]*t[i,j,c,d]*v[k,a,d,c],\{k,c,d\}] - \text{sum}[t[j,d]*t[k,b]*v[k,a,d,c],\{k,c,d\}] + 2*\text{sum}[t[i,c]*t[j,k,b,d]*v[k,a,d,c],\{k,c,d\}] - \text{sum} \\ & [t[i,c]*t[j,k,d,b]*v[k,a,d,c],\{k,c,d\}] - \text{sum}[t[j,k,b,c]*v[k,a,i,c],\{k,c\}] - \text{sum}[t[i,c]*t[k,b]*v[k,a,j,c],\{k,c\}] - \text{sum} \\ & [t[i,c]*t[j,d]*t[k,a]*v[k,b,c,d],\{k,c,d\}] - \text{sum}[t[k,d]*t[i,j,a,c]*v[k,b,c,d],\{k,c,d\}] - \text{sum}[t[k,a]*t[i,j,c,d]*v[k,b,c,d],\{k,c,d\}] \\ & + 2*\text{sum}[t[j,d]*t[i,k,a,c]*v[k,b,c,d],\{k,c,d\}] - \text{sum}[t[j,d]*t[i,k,c,a]*v[k,b,c,d],\{k,c,d\}] - \text{sum}[t[i,c]*t[j,k,d,a]*v[k,b,c,d],\{k,c,d\}] - \text{sum} \\ & [t[i,c]*t[k,a]*v[k,b,c,j],\{k,c\}] + 2*\text{sum}[t[i,k,a,c]*v[k,b,c,j],\{k,c\}] - \text{sum}[t[i,k,c,a]*v[k,b,c,j],\{k,c\}] \\ & + 2*\text{sum}[t[k,d]*t[i,j,a,c]*v[k,b,d,c],\{k,c,d\}] - \text{sum}[t[j,d]*t[i,k,a,c]*v[k,b,d,c],\{k,c,d\}] - \text{sum}[t[j,c]*t[k,a]*v[k,b,i,c],\{k,c\}] - \text{sum} \\ & [t[j,k,c,a]*v[k,b,i,c],\{k,c\}] - \text{sum}[t[i,k,a,c]*v[k,b,j,c],\{k,c\}] + \text{sum}[t[i,c]*t[j,d]*t[k,a]*t[l,b]*v[k,l,c,d],\{k,l,c,d\}] - 2*\text{sum} \\ & [t[k,b]*t[l,d]*t[i,j,a,c]*v[k,l,c,d],\{k,l,c,d\}] - 2*\text{sum}[t[k,a]*t[l,d]*t[i,j,c,b]*v[k,l,c,d],\{k,l,c,d\}] \\ & + \text{sum}[t[k,a]*t[l,b]*t[i,j,c,d]*v[k,l,c,d],\{k,l,c,d\}] - 2*\text{sum}[t[j,c]*t[l,d]*t[i,k,a,b]*v[k,l,c,d],\{k,l,c,d\}] - 2*\text{sum} \\ & [t[j,d]*t[l,b]*t[i,k,a,c]*v[k,l,c,d],\{k,l,c,d\}] + \text{sum}[t[j,c]*t[l,d]*t[i,k,c,a]*v[k,l,c,d],\{k,l,c,d\}] - 2*\text{sum} \\ & [t[i,c]*t[l,d]*t[j,k,b,a]*v[k,l,c,d],\{k,l,c,d\}] + \text{sum}[t[i,c]*t[l,a]*t[j,k,b,d]*v[k,l,c,d],\{k,l,c,d\}] \\ & + \text{sum}[t[i,c]*t[l,b]*t[j,k,d,a]*v[k,l,c,d],\{k,l,c,d\}] + \text{sum}[t[i,k,c,d]*t[j,l,b,a]*v[k,l,c,d],\{k,l,c,d\}] \\ & + 4*\text{sum}[t[i,k,a,c]*t[j,l,b,d]*v[k,l,c,d],\{k,l,c,d\}] - 2*\text{sum}[t[i,k,c,a]*t[j,l,b,d]*v[k,l,c,d],\{k,l,c,d\}] - 2*\text{sum} \\ & [t[i,k,a,b]*t[j,l,c,d]*v[k,l,c,d],\{k,l,c,d\}] - 2*\text{sum}[t[i,k,a,c]*t[j,l,d,b]*v[k,l,c,d],\{k,l,c,d\}] + \text{sum}[t[i,k,c,a]*t[j,l,d,b]*v[k,l,c,d],\{k,l,c,d\}] \\ & + \text{sum}[t[i,c]*t[j,d]*t[k,l,a,b]*v[k,l,c,d],\{k,l,c,d\}] + \text{sum}[t[i,j,c,d]*t[k,l,a,b]*v[k,l,c,d],\{k,l,c,d\}] - 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Tensor Contraction Engine (TCE)

- High-level domain-specific language for a class of problems in quantum chemistry/physics based on contraction of large multi-dimensional tensors
- Specialized optimizing compiler
 - Produces F77+GA code, linked to runtime libs

```
range V = 3000;
range O = 100;
index a,b,c,d,e,f : V;
index i,j,k,l : O;
mlimit = 100GB;

procedure P(in A[V,V,O,O], in B[V,V,V,O],
            in C[V,V,O,O], in D[V,V,V,O],
            out S[V,V,O,O])=
begin
  S[a,b,i,j] == sum[ A[a,c,i,k] * B[b,e,f,l]
                    * C[d,f,j,k] * D[c,d,e,l],
                    {c,e,f,k,l}];
end
```

$$S_{abij} = \sum_{cefk} A_{acik} B_{befl} C_{dfjk} D_{cdel}$$


NWChem CCSD(T) performance

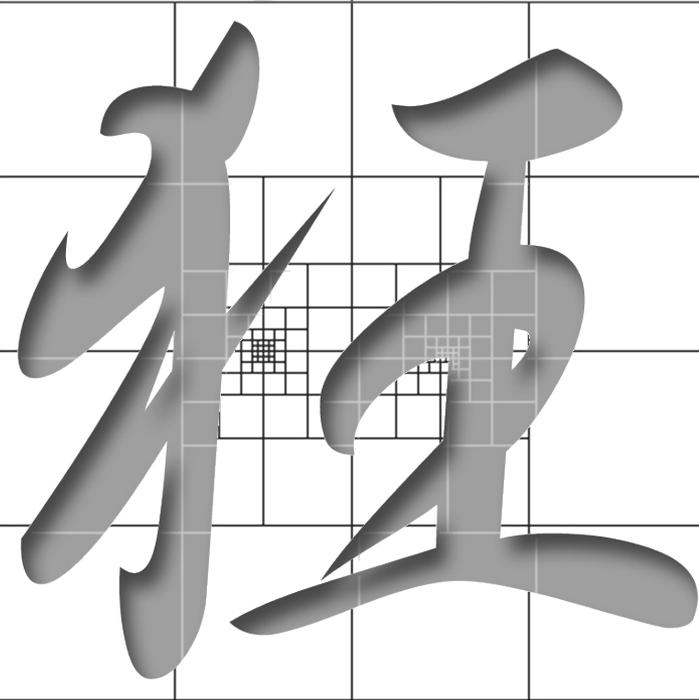
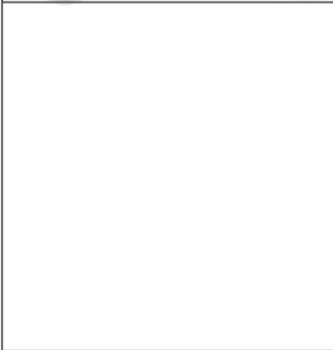
- Performed with NWChem by EMSL staff
- Closed-shell CCSD(T) calculations
 - Hand-written code
 - Octane (1468 basis functions, aug-cc-pVQZ) [Pollack, 2005].
 - Perturbative triples (T) took 23 hours on 1400 processors, yielding 75% CPU efficiency and a sustained performance of 6.3 TFlops. Fourteen iterations were required for convergence of the CCSD, which took approximately 43 hours on 600 processors.
 - Water cluster
 - Perturbative triples (T) took 28 hours on 1840 processors, yielding 84% CPU efficiency and a sustained performance of 11.04 TF.
- Large open-shell CCSD(T)
 - TCE machine-generated code
 - CF₃CHFO* (605 basis functions, aug-cc-pVQZ)
 - 19 hours with 1024 processors
- Example target system for petaflop
 - W₃O₉⁻ which has 678 basis functions with the aug-cc-pVTZ/ECP(W) basis set and close to 1400 basis functions with the aug-cc-pVTZ/ECP(W) basis set
 - These are single point calculations and geometry optimizations and frequency calculations are even more costly yet necessary.

M

A

D

N



T



Multiresolution
Adaptive
Numerical
Scientific
Simulation

S



S

Multiresolution Adaptive Numerical Scientific Simulation

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Multiresolution chemistry objectives

- Complete elimination of the basis error
 - One-electron models (e.g., HF, DFT)
 - Pair models (e.g., MP2, CCSD, ...)
- Correct scaling of cost with system size
- General approach
 - Readily accessible by students and researchers
 - Higher level of composition
 - Direct computation of chemical energy differences
- New computational approaches
- *Fast algorithms with guaranteed precision*

Essential techniques for fast computation

- Multiresolution $V_0 \quad V_1 \quad \mathbf{L} \quad V_n$

$$V_n = V_0 + (V_1 - V_0) + \mathbf{L} + (V_n - V_{n-1})$$
- Low-separation rank

$$f(x_1, \mathbf{K}, x_d) = \sum_{l=1}^M \sigma_l \prod_{i=1}^d f_i^{(l)}(x_i) + O(\varepsilon)$$

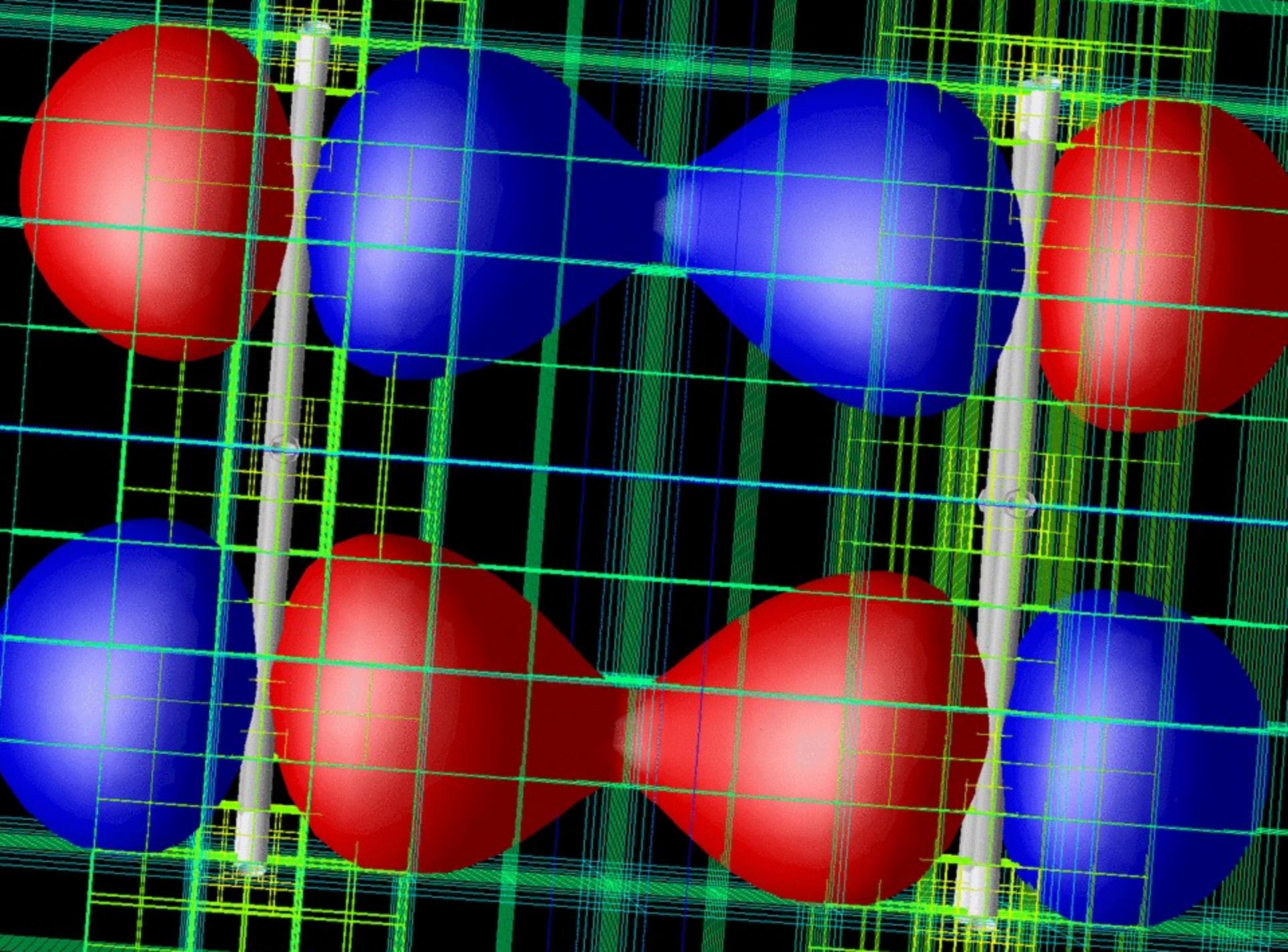
$$\|f_i^{(l)}\|_2 = 1 \quad \sigma_l > 0$$
- Low-operator rank

$$A = \sum_{\mu=1}^r \underline{u}_\mu \sigma_\mu \underline{v}_\mu^T + O(\varepsilon)$$

$$\sigma_\mu > 0 \quad \underline{v}_\mu^T \cdot \underline{v}_\lambda = \underline{u}_\mu^T \cdot \underline{u}_\lambda = \delta_{\mu\lambda}$$

Please forget about wavelets

- They are not central
- Wavelets are a convenient basis for spanning $V_n - V_{n-1}$ and understanding its properties
- But you don't actually need to use them
 - MADNESS does still compute wavelet coefficients, but *Beylkin's new code does not*
- Please remember this ...
 - Discontinuous spectral element with multi-resolution and separated representations for fast computation with guaranteed precision.



Current applications

- DFT & HF for electrons
 - Energies, gradients, excitation energies, non-linear optical properties, ...
 - Catalysis, nano-scale chemistry
- MCSCF
 - Time evolution of few-electron systems
- 6D prototype
 - Exact solution of 2-electron problem without use of any special symmetry
- Nuclear structure

High-level composition using functions and operators

- Conventional quant. chem. uses explicitly indexed sparse arrays of matrix elements
 - Complex, tedious and error prone

- Python classes for Function and Operator

- in 1,2,3,6 and general dimensions

- wide range of operations

`Hpsi = -0.5*DelSq*psi + V*psi`

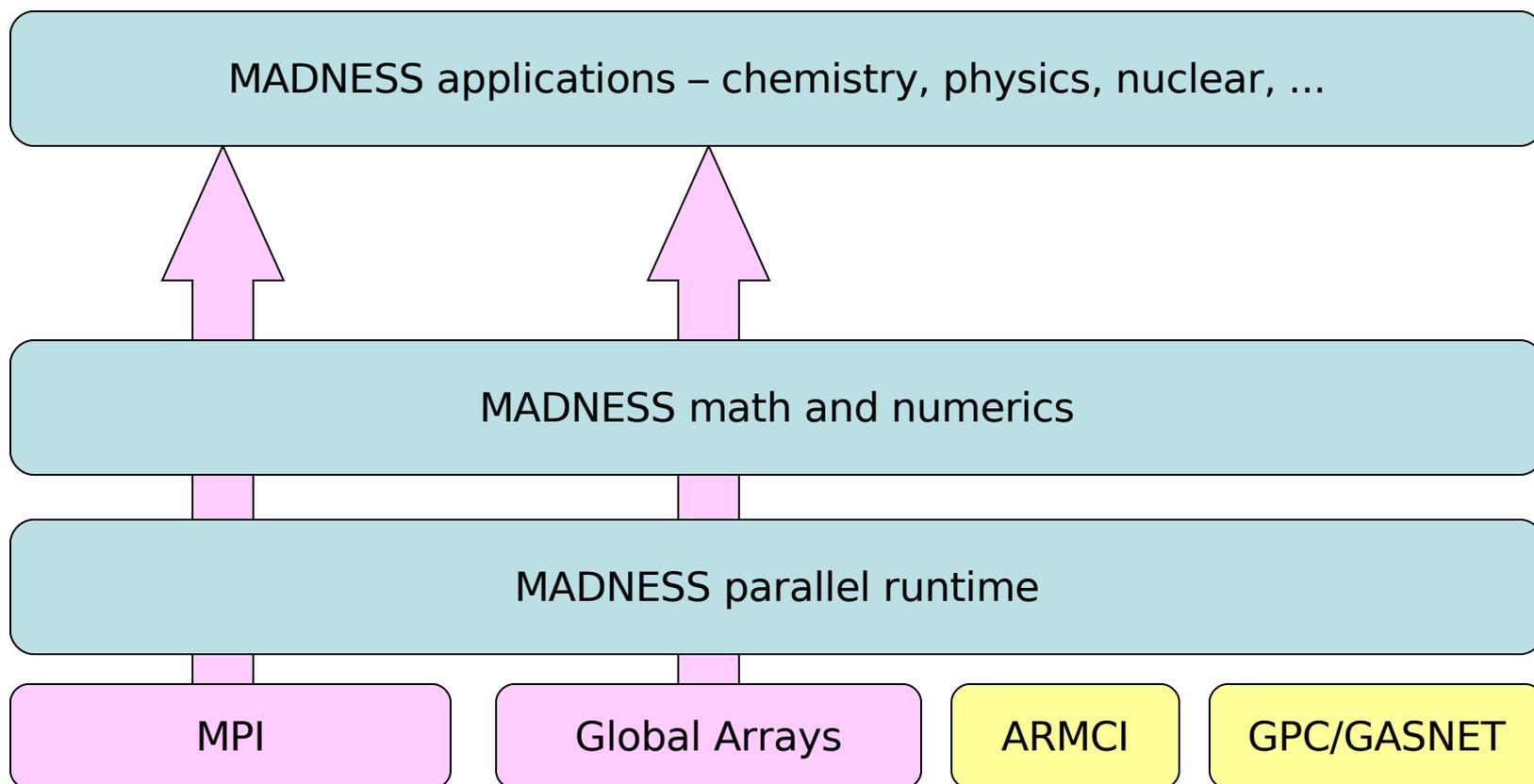
`J = Coulomb.apply(rho)`

$$H\varphi = -\frac{1}{2} \nabla^2 \varphi + V\varphi$$

$$J(r) = G * \rho$$

- All with guaranteed speed and precision $= \frac{\rho(s)}{|r-s|} ds$

MADNESS architecture



Runtime Objectives

- Scalability to 1+M processors ASAP
- Runtime responsible for
 - scheduling and placement,
 - managing data dependencies,
 - hiding latency, and
 - Medium to coarse grain concurrency
- Compatible with existing models
 - MPI, Global Arrays
- Borrow successful concepts from Cilk, Charm++, Python
- Anticipating next gen. languages

Key elements

- Futures for hiding latency and automating dependency management
- Global names and name spaces
- Non-process centric computing
 - One-sided messaging between objects
 - Retain place=process for MPI legacy
- Dynamic load balancing

Futures

- Result of an asynchronous computation
 - Cilk, Java, HPCLs
- Hide latency due to communication or computation
- Management of dependencies
 - Via callbacks

```
int f(int arg);
ProcessId me, p;

Future<int> r0=task(p, f, 0);
Future<int> r1=task(me, f, r0);

// Work until need result

cout << r0 << r1 << endl;
```

Process “me” spawns a new task in process “p” to execute $f(0)$ with the result eventually returned as the value of future $r0$. This is used as the argument of a second task whose execution is deferred until its argument is assigned. Tasks and futures can register multiple local or remote callbacks to express complex and dynamic dependencies.

Global Names

- Objects with global names with different state in each process

- C.f. shared[threads] in UPC; co-Array

```
class A : public WorldObject<A>{  
    int f(int) ;  
};  
ProcessID p;  
A a;  
Future<int> a.task(p, &A::f, 0);
```

- Non-collective constructor;
deferred destructor
- Eliminates synchronization

A task is sent to the instance of a in process p. If this has not yet been constructed the message is stored in a pending queue. Destruction of a global object is deferred until the next user synchronization point.

Global Namespaces

- Specialize global names to containers
 - Hash table done
 - Arrays, etc., planned
- Replace global pointer (process+local pointer) with more powerful concept
- User definable map from keys to “owner” process

```
class Index; // Hashable
class Value {
    double f(int);
};
```

```
WorldContainer<Index, Value> c;
Index i, j; Value v;
c.insert(i, v);
Future<double> =
    c.task(j, &Value::f, 666);
```

A container is created mapping indices to values.

A value is inserted into the container.

A task is spawned in the process owning key j to invoke $c[j].f(666)$.

Abstraction Overheads

- If you are careful you win
 - *Increased performance and productivity*
 - This is the lesson of Global Arrays, Charm++, ...
- Creating, executing, reaping a local, null task – 350us (100K tasks, 3GHz Core2, Pathscale 3.0, -Ofast) dominated by new/delete
- Chain of 100K dependent tasks with the result of a task as the unevaluated argument of the previous task
 - ~1 us per task
- Creating a remote task adds overhead of inter-process communication which is on the scale of 3us (Cray XT).
 - Aggregation can reduce this.
- Switching between user-space threads <20ns

Work in progress

- Multiple kernel threads for multi-core
- Full integration of Global Arrays
- Port to GPC and/or GASNET
- Interfaces to external solvers
- Dynamic load balance via work stealing
- Planned
 - Multiple user threads per kernel thread to reduce need for manual closures
 - Near-optimal global scheduling via DAG
 - Interfaces from C++ to Python and Octave