

Computational Atomic and Molecular Physics for Transport Modeling of Fusion Plasmas

M S Pindzola¹, F J Robicheaux¹, J P Colgan¹, S D Loch¹, J Ludlow¹, D R Schultz², T Mimami², J T Hogan², D C Griffin³, C P Ballance³, T Evans⁴, N R Badnell⁵, H P Summers⁵, A D Whiteford⁵, B M McLaughlin⁶, P G Burke⁶ and K A Berrington⁷

¹Dept of Physics, Auburn University, Auburn, AL ²Physics Division, Oak Ridge National Laboratory, TN

³Dept of Physics, Rollins College, FL ⁴DIII-D, General Atomics, CA ⁵Dept of Physics, Univ. of Strathclyde

⁶School of Mathematics & Physics, Queen's University of Belfast ⁷Dept of Mathematics, Sheffield Hallam University

ITER relevant modeling efforts

- Numerous issues are now pertinent in the run up to **ITER** operation. A DOE Scientific Discovery through Advanced Computing (**SDSC/DOE**) program has brought together a US-UK collaboration to implement state-of-the-art atomic collision codes on the next generation of resolvable computing facilities, to assist in answering questions such as
 - The final choice for **plasma-facing materials**, in particular the possible use of
 - Be, C, and W components for the first wall
 - Relevance of ionizations on operational regimes
 - Study of **ELM** transient in standard ITER operation



Figure 1: Schematic of ITER.

Plasma transport codes (such as **SOUPs**, **SANCO**) provide an insight into the transport of plasma impurities, the radiated power loss from various plasma impurity mixtures, and the behavior of ELM and transport barriers. These codes require good atomic data for

- effective ionization and recombination rate coefficients to track the ionization balance, and hence the plasma transport of impurity species
- emissivity coefficients to predict radiated power losses, and to compare with spectral observations.

Collisional-Radiative Modeling using ADAS

A modeling suite of codes called **ADAS** (Atomic Data and Analysis Structure) processes fundamental atomic data into a form useful for such transport codes, which are then used at facilities such as JET, ASDEX Upgrade, DIII-D, JT-60U, Tore-Supra and Alcator C-Mod.

- Solution to collisional-radiative equations to get the emitting population requires:
 - Atomic structure for **energies**, **radiative rate coefficients**
 - Collisional electron **excitation**, **ionization** and **recombination** rate coefficients
 - Collisional **charge transfer recombination** with neutral beam species
- Various coefficients are produced from the ADAS codes, which can be transparently used in transport codes, namely:
 - Effective ionization and recombination rate coefficients
 - Excitation and ionization cross sections
 - Spontaneous and induced emission coefficients
 - Charge transfer cross sections

Generalised collisional-radiative coefficients

- Radiated power loss coefficients
 - Plasma emissivity coefficients
 - Photoionisation cross sections
- We have completed calculations for the following systems
- He, Li and Be

However, the accuracy of the coefficients which are passed to the transport codes is directly related to the atomic data which is used to generate them. This much work has been done on generating highly accurate atomic data for key fusion species. These calculations are pushing the limits of current large scale computational resources, and are opening up new frontiers in atomic collision theory. We present some of these calculations in the following sections.

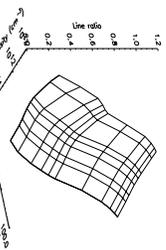


Figure 1: He (Li, Be) $n \rightarrow 1g^2$ / $n \rightarrow 1g, 2p$ rate ratio as calculated by the ADAS codes. The plot shows the rate ratio as a function of electron density and temperature. The theoretical limit ratio is one (dotted line) and represents a significant increase in data quality over existing data.

AM Calculations: Time dependent Semi-Classical

- Electron modeled as moving in the field of two moving Coulomb fields
- Especially useful for **charge transfer** cross sections, of relevance for fusion studies
- Applications such as $p-H$, $p-Li$, $\alpha + H$, $Be^{2+}-H$, $p-H^+$

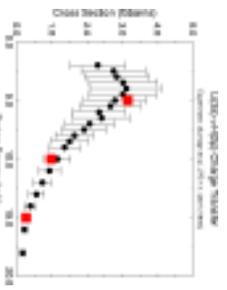


Figure 8: Semi-empirical charge transfer cross section of protons on ground state Helium

AM Calculations: Time independent R-Matrix

- Developed in the UK by P.C. Burke and co-workers, the method can be used to generate electron collisional **excitation**, **ionization** and **recombination** cross sections.
- All eigenvalues and eigenfunctions of 50,000 x 50,000 matrices are required. Thousands of energies are needed to map out the Resonance resonance structure. This can only be achieved on modern massively parallel computers.

R-Matrix with pseudostates calculations are completed for

- He, He⁺, Li, Li⁺, Li²⁺
- Be, Be⁺, Be²⁺, Be³⁺
- B⁺, B²⁺, C⁺, C²⁺, C³⁺, O⁺

Standard R-Matrix calculations are completed for

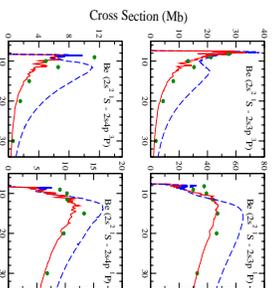


Figure 1: Electron collision cross sections for Be from the most reliable calculations. The effects of including pseudo states can be clearly seen.

AM Calculations: Time dependent Close-Coupling

- Treats the three body Coulomb breakup exactly
- Close coupled set of 2D infinite equations
- Calculations are completed for
 - H, He, He⁺, Li, Li⁺, Li²⁺
 - Be, Be⁺, Be²⁺, Be³⁺
 - B⁺, C⁺, Mg⁺, Al⁺, Si⁺
- Have now started to treat
 - four body Coulomb breakup problem
 - the threshold two Coulomb center breakup problem

AM Calculations: Distorted-wave and Classical Trajectory

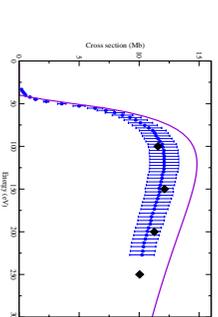


Figure 6: e^+ ionization cross section. The experimental results are shown in the blue circles and have been fitted with the theory. The solid line shows the distorted-wave calculation and the dashed line shows the classical trajectory method. The inset shows the theoretical results for the ionization cross section with significant relative error in the beam.

The distorted-wave techniques use perturbation theory

- They are accurate for **radiative** and **autoionization** rates, and for **electron collision** with highly charged ions
- There are various levels of calculation
 - Intermediate coupled distorted-wave (ICDW)
 - LS coupled distorted-wave (LSDW)
 - Configuration-average distorted-wave (CAIW)
 - Classical Trajectory Monte Carlo (CTMC)

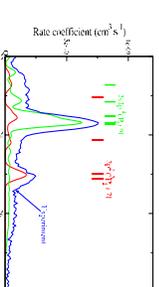


Figure 9: The rate coefficient of radiative recombination, as seen in CTMC.

Applications of our data

- Data we have generated is in use at various institutes
 - ASDEX Upgrade: Tungsten ionization data is to be used in heavy species studies
 - EPDA-JET: Helium excitation data we generated is in use in He beam studies
 - RFX: Krypton ionization data we made is in use in impurity transport studies
 - DIII-D: Lithium effective ionization and recombination data is being used for impurity transport studies

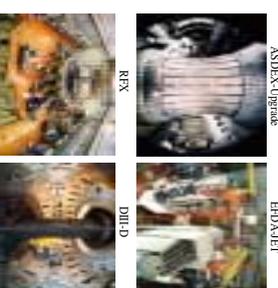


Figure 10: Images of various tokamak experiments and data being used

General science spin-offs

The advancements made as part of the work presented here, has also allowed progress to be made in other scientific areas, providing a valuable benchmarking of the codes. Some of these spin-offs include

- Photoionization of atoms and molecules
- RAPPS for (γ, ν) atoms and molecules
- TOOC for $(\gamma, 2\nu)$ on He, Be, Li⁺, quantum dots, H₂, (2 ν , 2 ν) on He, (3 ν , 3 ν) on Li
- TOOC for $e^+ + H$, TDSC for p-H and BEC in solids, CTMC for $e^+ +$ atoms in ultracold plasmas, $\gamma +$ atoms in high Rydberg states

Conclusions

- High quality atomic data is being processed into a form useful for **plasma transport modeling** and **excitation** and **ELM** experimental studies
- Recent advances in non-perturbative methods allows high quality atomic data to be generated for electron-ion and ion-ion collisions for low Z systems
- DW calculations provide high quality DR data for medium Z systems, and high quality electron ionization and excitation data for species such as tungsten

Fig. 1.—

Fig. 2.—

Fig. 3.—

Fig. 4.—

Fig. 5.—

Fig. 6.—

Fig. 7.—

Fig. 8.—

Fig. 9.—